

$$1) z \cdot \bar{z} = x^2 + y^2 \rightarrow \text{Real}$$

$$2) \omega = \frac{-1 + \sqrt{3}i}{2} \quad \omega^2 = \bar{\omega} = \frac{-1 - \sqrt{3}i}{2}$$

$$3) a\bar{\omega} + b\bar{\omega}^2 + c = a\omega^2 + b\omega + c$$

⊙ MODULUS OF A COMPLEX NO.

$$z = x + iy$$

$$|z|^2 = z \cdot \bar{z} = (x + iy)(x - iy) = x^2 + y^2$$

$$|z| = \sqrt{x^2 + y^2}$$

⊙ ARGUMENT OF A COMPLEX NO.

$$\arg(z) \rightarrow \pi/3, -\pi/3, \dots \quad \{\text{principal value}\}$$

$$\text{Arg}(z) = 2n\pi + \pi/3 \quad \{\text{general value}\}$$

$\arg(z)$ b/w 0 and π

$$\arg(z_1 \cdot z_2) = \arg z_1 + \arg z_2$$

⊙ TRIANGLE INEQUALITY

$$|z_1| + |z_2| \geq |z_1 \pm z_2| \quad \begin{array}{l} \text{(- sign for adjustment)} \\ \text{eg - } 2+i - (3-i) \\ \rightarrow 2+i + (-3+i) \end{array}$$

$$|z_1| - |z_2| \leq |z_1 \pm z_2|$$

$$z + \bar{z} = 2\text{Re}(z)$$

$$z - \bar{z} = 2\text{Im}(z)$$