

## 2.1

## Semiconductor Physics

In the problems assume the parameter given in following table. Use the temperature  $T = 300$  K unless otherwise stated.

Property	Si	GaAs	Ge
Bandgap Energy	1.12	1.42	0.66
Dielectric Constant	11.7	13.1	16.0
Effective density of states in conduction band $N_c$ ( $\text{cm}^{-3}$ )	$2.8 \times 10^{19}$	$4.7 \times 10^{17}$	$1.04 \times 10^{19}$
Effective density of states in valence band $N_v$ ( $\text{cm}^{-3}$ )	$1.04 \times 10^{19}$	$7.0 \times 10^{18}$	$6.0 \times 10^{18}$
Intrinsic carrier concentration $n_i$ ( $\text{cm}^{-3}$ )	$1.5 \times 10^{10}$	$1.8 \times 10^6$	$2.4 \times 10^{18}$
Mobility			
Electron	1350	8500	3900
Hole	480	400	1900

1. In germanium semiconductor material at  $T = 400$  K the intrinsic concentration is

- (A)  $26.8 \times 10^{14} \text{ cm}^{-3}$                       (B)  $18.4 \times 10^{14} \text{ cm}^{-3}$   
 (C)  $8.5 \times 10^{14} \text{ cm}^{-3}$                       (D)  $3.6 \times 10^{14} \text{ cm}^{-3}$

2. The intrinsic carrier concentration in silicon is to be no greater than  $n_i = 1 \times 10^{12} \text{ cm}^{-3}$ . The maximum temperature allowed for the silicon is (Assume  $E_g = 1.12 \text{ eV}$ )

- (A) 300 K                                      (B) 360 K  
 (C) 382 K                                      (D) 364 K

3. Two semiconductor material have exactly the same properties except that material A has a bandgap of 1.0

eV and material B has a bandgap energy of 1.2 eV. The ratio of intrinsic concentration of material A to that of material B is

- (A) 2016                                      (B) 47.5  
 (C) 58.23                                      (D) 1048

4. In silicon at  $T = 300$  K the thermal-equilibrium concentration of electron is  $n_0 = 5 \times 10^4 \text{ cm}^{-3}$ . The hole concentration is

- (A)  $4.5 \times 10^{15} \text{ cm}^{-3}$                       (B)  $4.5 \times 10^{15} \text{ m}^{-3}$   
 (C)  $0.3 \times 10^{-6} \text{ cm}^{-3}$                       (D)  $0.3 \times 10^{-6} \text{ m}^{-3}$

5. In silicon at  $T = 300$  K if the Fermi energy is 0.22 eV above the valence band energy, the value of  $p_0$  is

- (A)  $2 \times 10^{15} \text{ cm}^{-3}$                       (B)  $10^{15} \text{ cm}^{-3}$   
 (C)  $3 \times 10^{15} \text{ cm}^{-3}$                       (D)  $4 \times 10^{15} \text{ cm}^{-3}$

6. The thermal-equilibrium concentration of hole  $p_0$  in silicon at  $T = 300$  K is  $10^{15} \text{ cm}^{-3}$ . The value of  $n_0$  is

- (A)  $3.8 \times 10^8 \text{ cm}^{-3}$                       (B)  $4.4 \times 10^4 \text{ cm}^{-3}$   
 (C)  $2.6 \times 10^4 \text{ cm}^{-3}$                       (D)  $4.3 \times 10^8 \text{ cm}^{-3}$

7. In germanium semiconductor at  $T = 300$  K, the acceptor concentrations is  $N_a = 10^{13} \text{ cm}^{-3}$  and donor concentration is  $N_d = 0$ . The thermal equilibrium concentration  $p_0$  is

- (A)  $2.97 \times 10^9 \text{ cm}^{-3}$                       (B)  $2.68 \times 10^{12} \text{ cm}^{-3}$   
 (C)  $2.95 \times 10^{13} \text{ cm}^{-3}$                       (D)  $2.4 \text{ cm}^{-3}$

### Statement for Q.8-9:

In germanium semiconductor at  $T = 300$  K, the impurity concentration are

$$N_d = 5 \times 10^{15} \text{ cm}^{-3} \text{ and } N_a = 0$$

8. The thermal equilibrium electron concentration  $n_0$  is

- (A)  $5 \times 10^{15} \text{ cm}^{-3}$  (B)  $1.15 \times 10^{11} \text{ cm}^{-3}$   
 (C)  $1.15 \times 10^9 \text{ cm}^{-3}$  (D)  $5 \times 10^6 \text{ cm}^{-3}$

9. The thermal equilibrium hole concentration  $p_0$  is

- (A)  $3.96 \times 10^{13}$  (B)  $1.95 \times 10^{13} \text{ cm}^{-3}$   
 (C)  $4.36 \times 10^{12} \text{ cm}^{-3}$  (D)  $3.96 \times 10^{13} \text{ cm}^{-3}$

10. A sample of silicon at  $T = 300 \text{ K}$  is doped with boron at a concentration of  $2.5 \times 10^{13} \text{ cm}^{-3}$  and with arsenic at a concentration of  $1 \times 10^{13} \text{ cm}^{-3}$ . The material is

- (A)  $p$ -type with  $p_0 = 1.5 \times 10^{13} \text{ cm}^{-3}$   
 (B)  $p$ -type with  $p_0 = 1.5 \times 10^7 \text{ cm}^{-3}$   
 (C)  $n$ -type with  $n_0 = 1.5 \times 10^{13} \text{ cm}^{-3}$   
 (D)  $n$ -type with  $n_0 = 1.5 \times 10^7 \text{ cm}^{-3}$

11. In a sample of gallium arsenide at  $T = 200 \text{ K}$ ,  $n_0 = 5p_0$  and  $N_a = 0$ . The value of  $n_0$  is

- (A)  $9.86 \times 10^9 \text{ cm}^{-3}$  (B)  $7 \text{ cm}^{-3}$   
 (C)  $4.86 \times 10^3 \text{ cm}^{-3}$  (D)  $3 \text{ cm}^{-3}$

12. Germanium at  $T = 300 \text{ K}$  is uniformly doped with an acceptor concentration of  $N_a = 10^{15} \text{ cm}^{-3}$  and a donor concentration of  $N_d = 0$ . The position of fermi energy with respect to intrinsic Fermi level is

- (A) 0.02 eV (B) 0.04 eV  
 (C) 0.06 eV (D) 0.08 eV

13. In germanium at  $T = 300 \text{ K}$ , the donor concentration are  $N_d = 10^{14} \text{ cm}^{-3}$  and  $N_a = 0$ . The Fermi energy level with respect to intrinsic Fermi level is

- (A) 0.04 eV (B) 0.08 eV  
 (C) 0.42 eV (D) 0.86 eV

14. A GaAs device is doped with a donor concentration of  $3 \times 10^{15} \text{ cm}^{-3}$ . For the device to operate properly, the intrinsic carrier concentration must remain less than 5% of the total concentration. The maximum temperature on that the device may operate is

- (A) 763 K (B) 942 K  
 (C) 486 K (D) 243 K

15. For a particular semiconductor at  $T = 300 \text{ K}$   $E_g = 1.5 \text{ eV}$ ,  $m_p^* = 10m_n^*$  and  $n_i = 1 \times 10^{15} \text{ cm}^{-3}$ . The

position of Fermi level with respect to the center of the bandgap is

- (A) +0.045 eV (B) -0.046 eV  
 (C) +0.039 eV (D) -0.039 eV

16. A silicon sample contains acceptor atoms at a concentration of  $N_a = 5 \times 10^{15} \text{ cm}^{-3}$ . Donor atoms are added forming and  $n$ -type compensated semiconductor such that the Fermi level is 0.215 eV below the conduction band edge. The concentration of donors atoms added are

- (A)  $1.2 \times 10^{16} \text{ cm}^{-3}$  (B)  $4.6 \times 10^{16} \text{ cm}^{-3}$   
 (C)  $3.9 \times 10^{12} \text{ cm}^{-3}$  (D)  $2.4 \times 10^{12} \text{ cm}^{-3}$

17. A silicon semiconductor sample at  $T = 300 \text{ K}$  is doped with phosphorus atoms at a concentrations of  $10^{15} \text{ cm}^{-3}$ . The position of the Fermi level with respect to the intrinsic Fermi level is

- (A) 0.3 eV (B) 0.2 eV  
 (C) 0.1 eV (D) 0.4 eV

18. A silicon crystal having a cross-sectional area of  $0.001 \text{ cm}^2$  and a length of  $20 \mu\text{m}$  is connected to its ends to a 20 V battery. At  $T = 300 \text{ K}$ , we want a current of 100 mA in crystal. The concentration of donor atoms to be added is

- (A)  $2.4 \times 10^{13} \text{ cm}^{-3}$  (B)  $4.6 \times 10^{13} \text{ cm}^{-3}$   
 (C)  $7.8 \times 10^{14} \text{ cm}^{-3}$  (D)  $8.4 \times 10^{14} \text{ cm}^{-3}$

19. The cross sectional area of silicon bar is  $100 \mu\text{m}^2$ . The length of bar is 1 mm. The bar is doped with arsenic atoms. The resistance of bar is

- (A) 2.58 m $\Omega$  (B) 11.36 k $\Omega$   
 (C) 1.36 m $\Omega$  (D) 24.8 k $\Omega$

20. A thin film resistor is to be made from a GaAs film doped  $n$ -type. The resistor is to have a value of 2 k $\Omega$ . The resistor length is to be  $200 \mu\text{m}$  and area is to be  $10^{-6} \text{ cm}^2$ . The doping efficiency is known to be 90%. The mobility of electrons is 8000  $\text{cm}^2/\text{V}\cdot\text{s}$ . The doping needed is

- (A)  $8.7 \times 10^{15} \text{ cm}^{-3}$  (B)  $8.7 \times 10^{21} \text{ cm}^{-3}$   
 (C)  $4.6 \times 10^{15} \text{ cm}^{-3}$  (D)  $4.6 \times 10^{21} \text{ cm}^{-3}$

21. A silicon sample doped  $n$ -type at  $10^{18} \text{ cm}^{-3}$  have a resistance of 10  $\Omega$ . The sample has an area of  $10^{-6}$

$\text{cm}^2$  and a length of  $10 \mu\text{m}$ . The doping efficiency of the sample is ( $\mu_n = 800 \text{ cm}^2/\text{V-s}$ )

- (A) 43.2% (B) 78.1%  
(C) 96.3% (D) 54.3%

**22.** Six volts is applied across a 2 cm long semiconductor bar. The average drift velocity is  $10^4 \text{ cm/s}$ . The electron mobility is

- (A)  $4396 \text{ cm}^2/\text{V-s}$  (B)  $3 \times 10^4 \text{ cm}^2/\text{V-s}$   
(C)  $6 \times 10^4 \text{ cm}^2/\text{V-s}$  (D)  $3333 \text{ cm}^2/\text{V-s}$

**23.** For a particular semiconductor material following parameters are observed:

$$\mu_n = 1000 \text{ cm}^2/\text{V-s},$$

$$\mu_p = 600 \text{ cm}^2/\text{V-s},$$

$$N_c = N_v = 10^{19} \text{ cm}^{-3}$$

These parameters are independent of temperature. The measured conductivity of the intrinsic material is  $\sigma = 10^{-6} (\Omega\text{-cm})^{-1}$  at  $T = 300 \text{ K}$ . The conductivity at  $T = 500 \text{ K}$  is

- (A)  $2 \times 10^{-4} (\Omega\text{-cm})^{-1}$  (B)  $4 \times 10^{-5} (\Omega\text{-cm})^{-1}$   
(C)  $2 \times 10^{-5} (\Omega\text{-cm})^{-1}$  (D)  $6 \times 10^{-3} (\Omega\text{-cm})^{-1}$

**24.** An  $n$ -type silicon sample has a resistivity of  $5 \Omega\text{-cm}$  at  $T = 300 \text{ K}$ . The mobility is  $\mu_n = 1350 \text{ cm}^2/\text{V-s}$ . The donor impurity concentration is

- (A)  $2.86 \times 10^{-14} \text{ cm}^{-3}$  (B)  $9.25 \times 10^{14} \text{ cm}^{-3}$   
(C)  $11.46 \times 10^{15} \text{ cm}^{-3}$  (D)  $1.1 \times 10^{-15} \text{ cm}^{-3}$

**25.** In a silicon sample the electron concentration drops linearly from  $10^{18} \text{ cm}^{-3}$  to  $10^{16} \text{ cm}^{-3}$  over a length of  $2.0 \mu\text{m}$ . The current density due to the electron diffusion current is ( $D_n = 35 \text{ cm}^2/\text{s}$ ).

- (A)  $9.3 \times 10^4 \text{ A/cm}^2$  (B)  $2.8 \times 10^4 \text{ A/cm}^2$   
(C)  $9.3 \times 10^9 \text{ A/cm}^2$  (D)  $2.8 \times 10^9 \text{ A/cm}^2$

**26.** In a GaAs sample the electrons are moving under an electric field of  $5 \text{ kV/cm}$  and the carrier concentration is uniform at  $10^{16} \text{ cm}^{-3}$ . The electron velocity is the saturated velocity of  $10^7 \text{ cm/s}$ . The drift current density is

- (A)  $1.6 \times 10^4 \text{ A/cm}^2$  (B)  $2.4 \times 10^4 \text{ A/cm}^2$   
(C)  $1.6 \times 10^8 \text{ A/cm}^2$  (D)  $2.4 \times 10^8 \text{ A/cm}^2$

**27.** For a sample of GaAs scattering time is  $\tau_{sc} = 10^{-13} \text{ s}$  and electron's effective mass is  $m_e^* = 0.067 m_0$ . If an electric field of  $1 \text{ kV/cm}$  is applied, the drift velocity produced is

- (A)  $2.6 \times 10^6 \text{ cm/s}$  (B)  $263 \text{ cm/s}$   
(C)  $14.8 \times 10^6 \text{ cm/s}$  (D)  $482$

**28.** A gallium arsenide semiconductor at  $T = 300 \text{ K}$  is doped with impurity concentration  $N_d = 10^{16} \text{ cm}^{-3}$ . The mobility  $\mu_n$  is  $7500 \text{ cm}^2/\text{V-s}$ . For an applied field of  $10 \text{ V/cm}$  the drift current density is

- (A)  $120 \text{ A/cm}^2$  (B)  $120 \text{ A/cm}^2$   
(C)  $12 \times 10^4 \text{ A/cm}^2$  (D)  $12 \times 10^4 \text{ A/cm}^2$

**29.** In a particular semiconductor the donor impurity concentration is  $N_d = 10^{14} \text{ cm}^{-3}$ . Assume the following parameters,

$$\mu_n = 1000 \text{ cm}^2/\text{V-s},$$

$$N_c = 2 \times 10^{19} \left( \frac{T}{300} \right)^{3/2} \text{ cm}^{-3},$$

$$N_v = 1 \times 10^{19} \left( \frac{T}{300} \right)^{3/2} \text{ cm}^{-3},$$

$$E_g = 1.1 \text{ eV}.$$

An electric field of  $E = 10 \text{ V/cm}$  is applied. The electric current density at  $300 \text{ K}$  is

- (A)  $2.3 \text{ A/cm}^2$  (B)  $1.6 \text{ A/cm}^2$   
(C)  $9.6 \text{ A/cm}^2$  (D)  $3.4 \text{ A/cm}^2$

**Statement for Q.30-31:**

A semiconductor has following parameter

$$\mu_n = 7500 \text{ cm}^2/\text{V-s},$$

$$\mu_p = 300 \text{ cm}^2/\text{V-s},$$

$$n_i = 3.6 \times 10^{12} \text{ cm}^{-3}$$

**30.** When conductivity is minimum, the hole concentration is

- (A)  $7.2 \times 10^{11} \text{ cm}^{-3}$  (B)  $1.8 \times 10^{13} \text{ cm}^{-3}$   
(C)  $1.44 \times 10^{11} \text{ cm}^{-3}$  (D)  $9 \times 10^{13} \text{ cm}^{-3}$

**31.** The minimum conductivity is

- (A)  $0.6 \times 10^{-3} (\Omega\text{-cm})^{-1}$  (B)  $1.7 \times 10^{-3} (\Omega\text{-cm})^{-1}$   
(C)  $2.4 \times 10^{-3} (\Omega\text{-cm})^{-1}$  (D)  $6.8 \times 10^{-3} (\Omega\text{-cm})^{-1}$

**32.** A particular intrinsic semiconductor has a resistivity of  $50 (\Omega - \text{cm})$  at  $T = 300 \text{ K}$  and  $5 (\Omega - \text{cm})$  at  $T = 330 \text{ K}$ . If change in mobility with temperature is neglected, the bandgap energy of the semiconductor is

- (A) 1.9 eV (B) 1.3 eV  
(C) 2.6 eV (D) 0.64 eV

**33.** Three scattering mechanism exist in a semiconductor. If only the first mechanism were present, the mobility would be  $500 \text{ cm}^2/\text{V} - \text{s}$ . If only the second mechanism were present, the mobility would be  $750 \text{ cm}^2/\text{V} - \text{s}$ . If only third mechanism were present, the mobility would be  $1500 \text{ cm}^2/\text{V} - \text{s}$ . The net mobility is

- (A)  $2750 \text{ cm}^2/\text{V} - \text{s}$  (B)  $1114 \text{ cm}^2/\text{V} - \text{s}$   
(C)  $818 \text{ cm}^2/\text{V} - \text{s}$  (D)  $250 \text{ cm}^2/\text{V} - \text{s}$

**34.** In a sample of silicon at  $T = 300 \text{ K}$ , the electron concentration varies linearly with distance, as shown in fig. P2.1.34. The diffusion current density is found to be  $J_n = 0.19 \text{ A/cm}^2$ . If the electron diffusion coefficient is  $D_n = 25 \text{ cm}^2/\text{s}$ , The electron concentration at is

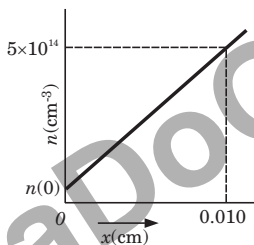


Fig. P2.1.34

- (A)  $4.86 \times 10^8 \text{ cm}^{-3}$  (B)  $2.5 \times 10^{13} \text{ cm}^{-3}$   
(C)  $9.8 \times 10^{26} \text{ cm}^{-3}$  (D)  $5.4 \times 10^{15} \text{ cm}^{-3}$

**35.** The hole concentration in  $p$ -type GaAs is given by

$$p = 10^{16} \left( 1 - \frac{x}{L} \right) \text{ cm}^{-3} \text{ for } 0 \leq x \leq L$$

where  $L = 10 \mu\text{m}$ . The hole diffusion coefficient is  $10 \text{ cm}^2/\text{s}$ . The hole diffusion current density at  $x = 5 \mu\text{m}$  is

- (A)  $20 \text{ A/cm}^2$  (B)  $16 \text{ A/cm}^2$   
(C)  $24 \text{ A/cm}^2$  (D)  $30 \text{ A/cm}^2$

**36.** For a particular semiconductor sample consider following parameters:

$$\text{Hole concentration } p_0 = 10^{15} e^{\left(\frac{-x}{L_p}\right)} \text{ cm}^{-3}, x \geq 0$$

$$\text{Electron concentration } n_0 = 5 \times 10^{14} e^{\left(\frac{-x}{L_n}\right)} \text{ cm}^{-3}, x \leq 0$$

$$\text{Hole diffusion coefficient } D_p = 10 \text{ cm}^2/\text{s}$$

$$\text{Electron diffusion coefficients } D_n = 25 \text{ cm}^2/\text{s}$$

$$\text{Hole diffusion length } L_p = 5 \times 10^{-4} \text{ cm},$$

$$\text{Electron diffusion length } L_n = 10^{-3} \text{ cm}$$

The total current density at  $x = 0$  is

- (A)  $1.2 \text{ A/cm}^2$  (B)  $5.2 \text{ A/cm}^2$   
(C)  $3.8 \text{ A/cm}^2$  (D)  $2 \text{ A/cm}^2$

**37.** A germanium Hall device is doped with  $5 \times 10^{15}$  donor atoms per  $\text{cm}^3$  at  $T = 300 \text{ K}$ . The device has the geometry  $d = 5 \times 10^{-3} \text{ cm}$ ,  $W = 2 \times 10^{-2} \text{ cm}$  and  $L = 0.1 \text{ cm}$ . The current is  $I_x = 250 \mu\text{A}$ , the applied voltage is  $V_x = 100 \text{ mV}$ , and the magnetic flux is  $B_z = 5 \times 10^{-2}$  tesla. The Hall voltage is

- (A)  $-0.31 \text{ mV}$  (B)  $0.31 \text{ mV}$   
(C)  $3.26 \text{ mV}$  (D)  $-3.26 \text{ mV}$

**Statement for Q.38-39:**

A silicon Hall device at  $T = 300 \text{ K}$  has the geometry  $d = 10^{-3} \text{ cm}$ ,  $W = 10^{-2} \text{ cm}$ ,  $L = 10^{-1} \text{ cm}$ . The following parameters are measured:  $I_x = 0.75 \text{ mA}$ ,  $V_x = 15 \text{ V}$ ,  $V_H = +5.8 \text{ mV}$ , tesla

**38.** The majority carrier concentration is

- (A)  $8 \times 10^{15} \text{ cm}^{-3}$ ,  $n$ -type  
(B)  $8 \times 10^{15} \text{ cm}^{-3}$ ,  $p$ -type  
(C)  $4 \times 10^{15} \text{ cm}^{-3}$ ,  $n$ -type  
(D)  $4 \times 10^{15} \text{ cm}^{-3}$ ,  $p$ -type

**39.** The majority carrier mobility is

- (A)  $430 \text{ cm}^2/\text{V} - \text{s}$  (B)  $215 \text{ cm}^2/\text{V} - \text{s}$   
(C)  $390 \text{ cm}^2/\text{V} - \text{s}$  (D)  $195 \text{ cm}^2/\text{V} - \text{s}$

**40.** In a semiconductor  $n_0 = 10^{15} \text{ cm}^{-3}$  and  $n_i = 10^{10} \text{ cm}^{-3}$ . The excess-carrier life time is  $10^{-6} \text{ s}$ . The excess hole concentration is  $\delta p = 4 \times 10^{13} \text{ cm}^{-3}$ . The electron-hole recombination rate is

- (A)  $4 \times 10^{19} \text{ cm}^{-3}\text{s}^{-1}$  (B)  $4 \times 10^{14} \text{ cm}^{-3}\text{s}^{-1}$   
(C)  $4 \times 10^{24} \text{ cm}^{-3}\text{s}^{-1}$  (D)  $4 \times 10^{11} \text{ cm}^{-3}\text{s}^{-1}$

41. A semiconductor in thermal equilibrium, has a hole concentration of  $p_0 = 10^{16} \text{ cm}^{-3}$  and an intrinsic concentration of  $n_i = 10^{10} \text{ cm}^{-3}$ . The minority carrier life time is  $4 \times 10^{-7} \text{ s}$ . The thermal equilibrium recombination rate of electrons is

- (A)  $2.5 \times 10^{22} \text{ cm}^{-3} \text{ s}^{-1}$       (B)  $5 \times 10^{10} \text{ cm}^{-3} \text{ s}^{-1}$   
 (C)  $2.5 \times 10^{10} \text{ cm}^{-3} \text{ s}^{-1}$       (D)  $5 \times 10^{22} \text{ cm}^{-3} \text{ s}^{-1}$

**Statement for Q.42-43:**

A n-type silicon sample contains a donor concentration of  $N_d = 10^{16} \text{ cm}^{-3}$ . The minority carrier hole lifetime is  $\tau_{p0} = 10 \mu\text{s}$ .

42. The thermal equilibrium generation rate of hole is

- (A)  $5 \times 10^8 \text{ cm}^{-3} \text{ s}^{-1}$       (B)  $10^4 \text{ cm}^{-3} \text{ s}^{-1}$   
 (C)  $2.25 \times 10^9 \text{ cm}^{-3} \text{ s}^{-1}$       (D)  $10^3 \text{ cm}^{-3} \text{ s}^{-1}$

43. The thermal equilibrium generation rate for electron is

- (A)  $1.125 \times 10^9 \text{ cm}^{-3} \text{ s}^{-1}$       (B)  $2.25 \times 10^9 \text{ cm}^{-3} \text{ s}^{-1}$   
 (C)  $8.9 \times 10^{-10} \text{ cm}^{-3} \text{ s}^{-1}$       (D)  $4 \times 10^9 \text{ cm}^{-3} \text{ s}^{-1}$

44. A n-type silicon sample contains a donor concentration of  $N_d = 10^{16} \text{ cm}^{-3}$ . The minority carrier hole lifetime is  $\tau_{p0} = 20 \mu\text{s}$ . The lifetime of the majority carrier is ( $n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$ )

- (A)  $8.9 \times 10^6 \text{ s}$       (B)  $8.9 \times 10^{-6} \text{ s}$   
 (C)  $4.5 \times 10^{-17} \text{ s}$       (D)  $1.13 \times 10^{-7} \text{ s}$

45. In a silicon semiconductor material the doping concentration are  $N_a = 10^{16} \text{ cm}^{-3}$  and  $N_d = 0$ . The equilibrium recombination rate is  $R_{p0} = 10^{11} \text{ cm}^{-3} \text{ s}^{-1}$ . A uniform generation rate produces an excess- carrier concentration of  $\delta n = \delta p = 10^{14} \text{ cm}^{-3}$ . The factor, by which the total recombination rate increase is

- (A)  $2.3 \times 10^{13}$       (B)  $4.4 \times 10^{13}$   
 (C)  $2.3 \times 10^9$       (D)  $4.4 \times 10^9$

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# Solutions

1. (D)  $n_i^2 = N_c N_v e^{-\left(\frac{E_g}{kT}\right)}$

$V_t = 0.0259 \left(\frac{400}{300}\right) = 0.0345$

For Ge at 300 K,

$N_c = 1.04 \times 10^{19}$ ,  $N_v = 6.0 \times 10^{18}$ ,  $E_g = 0.66 \text{ eV}$

$n_i^2 = 1.04 \times 10^{19} \times 6.0 \times 10^{18} \times \left(\frac{400}{300}\right)^3 \times e^{-\left(\frac{0.66}{0.0345}\right)}$

$\Rightarrow n_i = 8.5 \times 10^{14} \text{ cm}^{-3}$

2. (C)  $n_i^2 = N_c N_v e^{-\left(\frac{E_g}{kT}\right)}$

$(10^{12})^2 = 2.8 \times 10^{19} \times 1.04 \times 10^{19} \left(\frac{T}{300}\right)^3 e^{-\left(\frac{1.12e}{kT}\right)}$

$T^3 e^{-\frac{13 \times 10^3}{T}} = 928 \times 10^{-8}$ , By trial  $T = 382 \text{ K}$

3. (B)  $\frac{n_{iA}^2}{n_{iB}^2} = \frac{e^{-\frac{E_{gA}}{kT}}}{e^{-\frac{E_{gB}}{kT}}} = e^{-\left(\frac{E_{gA} - E_{gB}}{kT}\right)} = 2257.5 \Rightarrow \frac{n_{iA}}{n_{iB}} = 47.5$

4. (A)  $p_0 = \frac{n_i^2}{n_0} = \frac{(1.5 \times 10^{10})^2}{5 \times 10^4} = 4.5 \times 10^{15} \text{ cm}^{-3}$

5. (A)  $p_0 = N_v e^{-\frac{(E_F - E_v)}{kT}} = 1.04 \times 10^{19} e^{-\frac{0.22}{0.0259}} = 2 \times 10^{15} \text{ cm}^{-3}$

6. (B)  $p_0 = N_v e^{-\frac{(E_F - E_v)}{kT}} \Rightarrow E_F - E_v = kT \ln \left(\frac{N_v}{p_0}\right)$

At 300 K,  $N_v = 1.0 \times 10^{19} \text{ cm}^{-3}$

$E_F - E_v = 0.0259 \ln \left(\frac{1.04 \times 10^{19}}{10^{15}}\right) = 0.239 \text{ eV}$

$n_0 = N_c e^{-\frac{(E_c - E_F)}{kT}}$

At 300 K,  $N_c = 2.8 \times 10^{19} \text{ cm}^{-3}$

$E_c - E_F = 1.12 - 0.239 = 0.881 \text{ eV}$

$n_0 = 4.4 \times 10^4 \text{ cm}^{-3}$

7. (C)  $p_0 = \frac{N_a - N_d}{2} + \sqrt{\left(\frac{N_a - N_d}{2}\right)^2 + n_i^2}$

For Ge  $n_i = 2.4 \times 10^3$

$p_0 = \frac{10^{13}}{2} + \sqrt{\left(\frac{10^{13}}{2}\right)^2 + (2.4 \times 10^3)^2} = 2.95 \times 10^{13} \text{ cm}^{-3}$

$$8. (A) n_0 = \frac{N_d - N_a}{2} + \sqrt{\left(\frac{N_d - N_a}{2}\right)^2 + n_i^2}$$

$$= \frac{5 \times 10^{15}}{2} + \sqrt{\left(\frac{5 \times 10^{15}}{2}\right)^2 + (2.4 \times 10^{13})^2} = 5 \times 10^{15} \text{ cm}^{-3}$$

$$9. (B) p_0 = \frac{n_i^2}{p_0} = \frac{(2.4 \times 10^{13})^2}{2.95 \times 10^{13}} = 1.95 \times 10^{13} \text{ cm}^{-3}$$

10. (A) Since  $N_a > N_d$ , thus material is p-type ,  
 $p_0 = N_a - N_d = 2.5 \times 10^3 - 1 \times 10^3 = 1.5 \times 10^{13} \text{ cm}^{-3}$

$$11. (D) kT = 0.0259 \left(\frac{200}{300}\right) = 0.0173 \text{ eV}$$

For GaAs at 300 K,

$$N_c = 4.7 \times 10^{17} \text{ cm}^{-3}, \quad N_v = 7.0 \times 10^{18}, \quad E_g = 1.42 \text{ eV}$$

$$n_i^2 = 4.7 \times 10^{17} \times 7.0 \times 10^{18} \left(\frac{200}{300}\right)^3 e^{-\left(\frac{1.42}{0.0173}\right)}$$

$$\Rightarrow n_i = 1.48 \text{ cm}^{-3}$$

$$n_i^2 = n_0 p_0 = 5 p_0^2 = \frac{n_0^2}{5}$$

$$n_0 = \sqrt{5} n_i = 3.3 \text{ cm}^{-3}$$

$$12. (A) kT = 0.0259 \left(\frac{400}{300}\right) = 0.0345 \text{ eV}$$

$$n_i^2 = N_c N_v e^{-\left(\frac{E_g}{kT}\right)}$$

For Ge at 300 K,

$$N_c = 1.04 \times 10^{19} \text{ cm}^{-3}, \quad N_v = 6 \times 10^{18} \text{ cm}^{-3}, \quad E_g = 0.66 \text{ eV}$$

$$n_i^2 = 1.04 \times 10^{19} \times 6 \times 10^{18} \left(\frac{400}{300}\right)^3 e^{-\left(\frac{0.66}{0.0345}\right)} = 7.274 \times 10^{29}$$

$$n_i = 8.528 \times 10^{14} \text{ cm}^{-3}$$

$$p_0 = \frac{N_a}{2} + \sqrt{\left(\frac{N_a}{2}\right)^2 + n_i^2}$$

$$= \frac{10^{15}}{2} + \sqrt{\left(\frac{10^{15}}{2}\right)^2 + 7.274 \times 10^{29}}$$

$$\Rightarrow p_0 = 1.489 \times 10^{15} \text{ cm}^{-3}$$

$$E_{Fi} - E_F = kT \ln \left(\frac{p_0}{n_0}\right) = 0.0345 \ln \left(\frac{1.489 \times 10^{15}}{8.528 \times 10^{14}}\right)$$

$$= 0.019 \text{ eV}$$

$$13. (A) n_0 = \frac{N_d}{2} + \sqrt{\left(\frac{N_d}{2}\right)^2 + n_i^2}$$

For Ge at  $T = 300 \text{ K}$ ,  $n_i = 2.4 \times 10^{13} \text{ cm}^{-3}$

$$n_0 = \frac{10^{14}}{2} + \sqrt{\left(\frac{10^{14}}{2}\right)^2 + (2.4 \times 10^{13})^2} = 1.055 \times 10^{14} \text{ cm}^{-3}$$

$$E_F - E_{Fi} = kT \ln \left(\frac{n_0}{n_i}\right) = 0.0259 \ln \left(\frac{1.055 \times 10^{14}}{2.4 \times 10^{13}}\right)$$

$$= 0.0383 \text{ eV}$$

$$14. (A) n_0 = \frac{N_d}{2} + \sqrt{\left(\frac{N_d}{2}\right)^2 + n_i^2}$$

$$n_i = 0.05 n_0$$

$$\Rightarrow n_0 = 1.5 \times 10^{15} + \sqrt{(1.5 \times 10^{15})^2 + (0.05 n_0)^2}$$

$$\Rightarrow n_0 = 3.0075 \times 10^{15} \text{ cm}^{-3}$$

$$n_i = 1.504 \times 10^{14} \text{ cm}^{-3}$$

$$n_i^2 = N_c N_v e^{-\left(\frac{E_g}{kT}\right)}$$

For GaAs at  $T = 300 \text{ K}$ ,

$$N_c = 4.7 \times 10^{17}, \quad N_v = 7 \times 10^{18}, \quad E_g = 1.42 \text{ eV}$$

$$(1.504)^2 = 4.7 \times 10^{17} \times 7 \times 10^{18} \left(\frac{T}{300}\right)^3 e^{-\left(\frac{1.42 \times 300}{0.0259T}\right)}$$

By trial and error  $T = 763 \text{ K}$

$$15. (A) E_{Fi} - E_{midgap} = \frac{3}{4} kT \ln \left(\frac{m_p^*}{m_p}\right) = 0.0446 \text{ eV}$$

$$16. (A) n_0 = N_d - N_a = N_c e^{-\left(\frac{E_c - E_F}{kT}\right)}$$

For Si,  $N_c = 2.8 \times 10^{19} \text{ cm}^{-3}$

$$N_d = 5 \times 10^{15} + 2.8 \times 10^{19} e^{-\left(\frac{0.215}{0.0259}\right)} = 1.19 \times 10^{16} \text{ cm}^{-3}$$

$$17. (A) E_F - E_{Fi} = kT \ln \left(\frac{N_d}{N_i}\right)$$

$$= 0.0259 \ln \left(\frac{10^{15}}{1.5 \times 10^{10}}\right) = 0.287 \text{ eV}$$

$$18. (D) R = \frac{V}{I} = \frac{20}{100\text{m}} = 200 \Omega$$

$$\sigma = \frac{L}{RA} = \frac{2 \times 10^{-3}}{(200)(0.001)} = 0.01 (\Omega \text{ - cm})^{-1}$$

$\sigma \approx e \mu_n n_0$ , For Si,  $\mu_n = 1350$ .

$$\Rightarrow 0.01 = (1.6 \times 10^{-19})(1350)n_0$$

$$n_0 = 4.6 \times 10^{13} \text{ cm}^{-3},$$

$$n_0 \gg n_i \Rightarrow n_0 = N_d$$

19. (B)  $N_d \gg n_i \Rightarrow n_0 = N_d$ ,  $\sigma \approx e \mu_n n_0$ ,

$$R = \frac{L}{\sigma A} = \frac{L}{e \mu_n N_d A},$$

$$= \frac{0.1}{(1.6 \times 10^{-19})(1100)(5 \times 10^{16})(100 \times 10^{-8})} = 11.36 \text{ k}\Omega$$

$$20. \text{ (A) } R = \frac{L}{\sigma A}, \quad \sigma \approx e \mu_n n_0, \quad R = \frac{L}{e \mu_n n_0 A}$$

$$\Rightarrow n_0 = \frac{L}{e \mu_n AR}$$

$$n_0 = 0.9 N_d$$

$$= \frac{20 \times 10^{-4}}{(0.9)(1.6 \times 10^{-19})(8000)(10^{-6})(2 \times 10^3)} = 8.7 \times 10^{15} \text{ cm}^{-3}$$

$$21. \text{ (B) } \sigma \approx e \mu_n n_0, \quad R = \frac{L}{\sigma A}, \quad n_0 = \frac{L}{e \mu_n AR}$$

$$= \frac{10 \times 10^{-4}}{(1.6 \times 10^{-19})(800)(10^{-6})(10)} = 7.81 \times 10^{17} \text{ cm}^{-3}$$

$$\text{Efficiency} = \frac{n_0}{N_d} \times 100 = \frac{7.8 \times 10^{17}}{10^{18}} \times 100 = 78.1 \%$$

$$22. \text{ (D) } E = \frac{V}{L} = \frac{6}{2} = 3 \text{ V/cm}, \quad v_d = \mu_n E,$$

$$\mu_n = \frac{v_d}{E} = \frac{10^4}{3} = 3333 \text{ cm}^2/\text{V-s}$$

$$23. \text{ (D) } \sigma_1 = e n_i (\mu_n + \mu_p)$$

$$10^{-6} = (1.6 \times 10^{-19})(1000 + 600)n_i$$

$$\text{At } T = 300 \text{ K}, \quad n_i = 3.91 \times 10^9 \text{ cm}^{-3}$$

$$n_i^2 = N_c N_v e^{-\left(\frac{E_g}{kT}\right)} \Rightarrow E_g = kT \ln \left( \frac{N_c N_v}{n_i^2} \right)$$

$$\Rightarrow E_g = 2(0.0259) \ln \left( \frac{10^{19}}{3.91 \times 10^9} \right) = 1.122 \text{ eV}$$

$$\text{At } T = 500 \text{ K}, \quad kT = 0.0259 \left( \frac{500}{300} \right) = 0.0432 \text{ eV},$$

$$n_i^2 = (10^{19})^2 e^{-\left(\frac{1.122}{0.0432}\right)} \text{ cm}^{-3},$$

$$\Rightarrow n_i = 2.29 \times 10^{13} \text{ cm}^{-3}$$

$$= (1.6 \times 10^{-19})(2.29 \times 10^{13})(1000 + 600)$$

$$= 5.86 \times 10^{-3} (\Omega \text{ - cm})^{-1}$$

$$24. \text{ (B) } \rho = \frac{1}{\sigma} = \frac{1}{e \mu_n N_d}$$

$$N_d = \frac{1}{\rho e \mu_n} = \frac{1}{5(1.6 \times 10^{-19})(1350)} = 9.25 \times 10^{14} \text{ cm}^{-3}$$

$$25. \text{ (B) } J_n = e D_n \frac{dn}{dx}$$

$$= (1.6 \times 10^{-19})(35) \left( \frac{10^{18} - 10^{16}}{2 \times 10^{-4}} \right) = 2.8 \times 10^4 \text{ A/cm}^2$$

$$26. \text{ (A) } J = evn = (1.6 \times 10^{-19})(10^7)(10^{16}) = 1.6 \text{ A/cm}^2$$

$$27. \text{ (A) } v_d = \frac{e \tau_{sc} E}{m_e^*} = \frac{(1.6 \times 10^{-19})(10^{-13})(10^5)}{(0.067)(9.1 \times 10^{-31})}$$

$$= 262 \times 10^3 \text{ m/s} = 2.6 \times 10^6 \text{ cm/s}$$

$$28. \text{ (A) } N_d \gg n_i \Rightarrow n_0 = N_d$$

$$J = e \mu_n n_0 E = (1.6 \times 10^{-19})(7500)(10^{16})(10) = 120 \text{ A/cm}^2$$

$$29. \text{ (D) } n_i^2 = N_c N_v e^{-\left(\frac{E_g}{kT}\right)}$$

$$= (2 \times 10^{19})(1 \times 10^{19}) e^{-\left(\frac{1.1}{0.0259}\right)} = 7.18 \times 10^{19}$$

$$\Rightarrow n_i = 8.47 \times 10^9 \text{ cm}^{-3}$$

$$N_d \gg n_i \Rightarrow N_d = n_0$$

$$J = \sigma E = e \mu_n n_0 E$$

$$= (1.6 \times 10^{-19})(1000)(10^{14})(100) = 1.6 \text{ A/cm}^2$$

$$30. \text{ (A) } \sigma = e \mu_n n_0 + e \mu_p p_0 \text{ and } n_0 = \frac{n_i^2}{p_0}$$

$$\Rightarrow \sigma = e \mu_n \frac{n_i^2}{p_0} + e \mu_p p_0,$$

$$\frac{d\sigma}{dp_0} = 0 = \frac{(-1)e \mu_n n_i^2}{p_0^2} + e \mu_p$$

$$\Rightarrow p_0 = n_i \left( \frac{\mu_n}{\mu_p} \right)^{\frac{1}{2}} = 3.6 \times 10^{12} \left( \frac{7500}{300} \right)^{\frac{1}{2}}$$

$$= 7.2 \times 10^{11} \text{ cm}^{-3}$$

$$31. \text{ (B) } \sigma_{min} = \frac{2\sigma_i \sqrt{\mu_p \mu_n}}{\mu_p + \mu_n} = 2 e n_i \sqrt{\mu_p \mu_n}$$

$$= 2 \times 1.6 \times 10^{-19} (3.6 \times 10^{12}) \sqrt{(7500)(300)}$$

$$= 1.7 \times 10^{-3} (\Omega \text{ - cm})^{-1}$$

$$32. \text{ (B) } \sigma = \frac{1}{\rho} = e \mu n_i,$$

$$\frac{1}{\rho_1} = \frac{n_{i1}}{n_{i2}} = \frac{e^{-\frac{E_g}{2kT_1}}}{e^{-\frac{E_g}{2kT_2}}}$$

$$\frac{1}{\rho_2} = \frac{E_g \left( \frac{1}{T_1} - \frac{1}{T_2} \right)}{2k}$$

$$0.1 = e^{-\frac{E_g \left( \frac{1}{T_1} - \frac{1}{T_2} \right)}{2k}}$$

$$\frac{E_g}{2k} \left( \frac{330 - 300}{330 \times 300} \right) = \ln 10$$

$$E_g = 22(k300) \ln 10 = 1.31 \text{ eV}$$

$$33. \text{ (D) } \frac{1}{\mu} = \frac{1}{\mu_1} + \frac{1}{\mu_2} + \frac{1}{\mu_3}$$

$$\frac{1}{\mu} = \frac{1}{500} + \frac{1}{750} + \frac{1}{1500} \Rightarrow \mu = 250 \text{ cm}^2/\text{V-s}$$

$$34. \text{ (B) } J_n = eD_n \frac{dn}{dx}$$

$$0.19 = (1.6 \times 10^{-19})(25) \left( \frac{5 \times 10^{14} - n(0)}{0.010} \right)$$

$$n(0) = 2.5 \times 10^{13} \text{ cm}^{-3}$$

$$35. \text{ (B) } J = -eD_p \frac{dp}{dx} = -eD_p \frac{d}{dx} \left( 10^{16} \left( 1 - \frac{x}{L} \right) \right) = \frac{e10^{16}D_p}{L}$$

$$= \frac{(1.6 \times 10^{-19})(10^{16})(10)}{10 \times 10^{-4}}$$

$$J = 16 \text{ A/cm}^2$$

$$36. \text{ (B) } J_p = -eD_p \frac{dp_0}{dx} \Big|_{x=0} = \frac{10^{15}eD_p}{L_p}$$

$$J_n = eD_n \frac{dn_0}{dx} \Big|_{x=0} = \frac{5 \times 10^{14}eD_n}{L_n}$$

$$J = J_p + J_n = \frac{10^{15}eD_p}{L_p} + \frac{5 \times 10^{14}eD_n}{L_n}$$

$$= 1.6 \times 10^{-19} \left( \frac{10^{15}(10)}{15 \times 10^{-4}} + \frac{5 \times 10^{14}(25)}{10^{-3}} \right) = 5.2 \text{ A/cm}^2$$

$$37. \text{ (A) } V_H = \frac{-I_x B_z}{ned}$$

$$= \frac{(250 \times 10^{-6})(5 \times 10^{-2})}{(5 \times 10^{21})(1.6 \times 10^{-19})(5 \times 10^{-5})} = -0.313 \text{ mV}$$

38. (B)  $V_H$  is positive p-type

$$V_H = \frac{I_x B_z}{epd} \Rightarrow p = \frac{I_x B_z}{eV_H d}$$

$$p = \frac{(0.75 \times 10^{-3})(10^{-1})}{(1.6 \times 10^{-19})(5.8 \times 10^{-3})(10^{-5})}$$

$$= 8.08 \times 10^{21} \text{ m}^{-3} = 8.08 \times 10^{15} \text{ cm}^{-3}$$

$$39. \text{ (C) } u_p = \frac{I_x L}{epV_x W d}$$

$$= \frac{(0.75 \times 10^{-3})(10^{-3})}{(1.6 \times 10^{-19})(8.08 \times 10^{21})(15)(10^{-4})(10^{-5})}$$

$$\mu_p = 3.9 \times 10^{-2} \text{ m}^2/\text{V-s} = 390 \text{ cm}^2/\text{V-s}$$

40. (A) n-type semiconductor

$$R = \frac{\delta p}{\tau_{p0}} = \frac{4 \times 10^{13}}{10^{-6}} = 4 \times 10^{19} \text{ cm}^{-3}\text{s}^{-1}$$

$$41. \text{ (C) } n_0 = \frac{n_i^2}{p_0} = \frac{(10^{10})^2}{10^{16}} = 10^4 \text{ cm}^{-3}$$

$$R_{n0} = \frac{n_0}{\tau_{n0}} = \frac{10^4}{4 \times 10^{-7}} = 2.5 \times 10^{10} \text{ cm}^{-3}\text{s}^{-1}$$

$$42. \text{ (C) } R_{n0} = \frac{p_0}{\tau_{p0}}, p_0 = \frac{n_i^2}{n_0}, n_0 = N_d = 10^6 \text{ cm}^{-3}$$

$$p_0 = \frac{(1.5 \times 10^{10})^2}{10^{16}} = 2.25 \times 10^4 \text{ cm}^{-3}$$

$$R_{n0} = \frac{2.25 \times 10^4}{10 \times 10^{-6}} = 2.25 \times 10^9 \text{ cm}^{-3}\text{s}^{-1}$$

43. (B) Recombination rate for minority and majority carrier are equal. The generation rate is equal to Recombination rate.

$$G = R_{n0} = R_{p0} = 2.25 \times 10^9 \text{ cm}^{-3}\text{s}^{-1}$$

44. (A) Recombination rates are equal  $\frac{n_0}{\tau_{n0}} = \frac{p_0}{\tau_{p0}}$ ,

$$N_d \gg n_i$$

$$n_0 = N_d, p_0 = \frac{n_i^2}{n_0}$$

$$\tau_{n0} = \frac{n_0}{p_0} \tau_{p0} = \frac{n_0^2}{n_i^2} \tau_{p0}$$

$$= \left( \frac{10^{16}}{1.5 \times 10^{10}} \right)^2 \times 20 \times 10^{-6} = 8.9 \times 10^6 \text{ s}$$

45. (D)  $N_d \gg n_i \Rightarrow n_0 = N_d$

$$p_0 = \frac{n_i^2}{n_0} = \frac{(1.5 \times 10^{10})^2}{10^{16}} = 2.25 \times 10^4 \text{ cm}^{-3}$$

$$R_{p0} = \frac{p_0}{\tau_{p0}} \Rightarrow \tau_{p0} = \frac{p_0}{R_{p0}} = \frac{2.25 \times 10^4}{10^{11}} = 2.25 \times 10^7 \text{ s}$$

$$R_p = \frac{\delta p}{\tau_{p0}} = \frac{10^{14}}{2.25 \times 10^7} = 4.44 \times 10^{20} \text{ cm}^{-3}\text{s}^{-1}$$

$$\frac{R_p}{R_{p0}} = \frac{4.44 \times 10^{20}}{10^{11}} = 4.44 \times 10^9$$

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