



A HYBRID QUANTITATIVE–MANAGERIAL FRAMEWORK LINKING MATHEMATICAL MODELLING AND MANAGEMENT FOR CIRCULAR ECONOMY DESIGN AND IMPLEMENTATION

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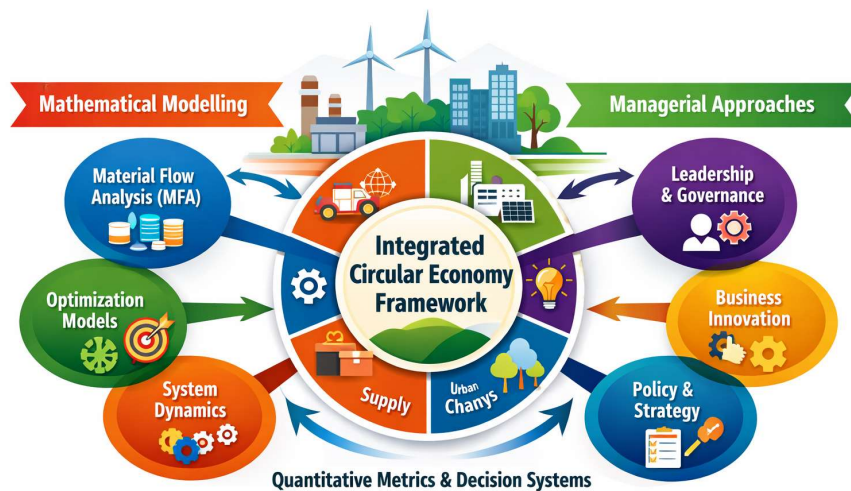
Abstract:

The transition toward sustainable development has positioned the circular economy (CE) as a central framework for addressing resource depletion, waste accumulation, and environmental degradation. Despite growing academic and industrial interest, CE implementation often remains fragmented due to limited quantitative modelling and weak managerial integration. This study presents an integrated mathematical–managerial framework for circular economy implementation by combining material flow analysis (MFA), optimization models, system dynamics, and strategic management approaches. The proposed hybrid framework links quantitative circularity metrics with managerial decision-making and governance structures, enabling organizations to translate analytical insights into operational action. The findings demonstrate that effective CE adoption depends not only on mathematical rigor but also on leadership commitment, organizational readiness, and policy alignment. The framework is applicable across manufacturing, supply chains, energy systems, and urban ecosystems, offering a scalable and decision-oriented pathway for advancing circular economy practices.

Keywords: Circular Economy; Mathematical Modelling; Material Flow Analysis; Optimization; System Dynamics; Managerial Approaches; Sustainable Supply Chains; Reverse Logistics; Life Cycle Assessment; Circular Business Models

Subject Classification:

Scopus Subject Areas, Environmental Science (Environmental Management; Waste Management; Sustainability), Engineering (Industrial and Systems Engineering), Business, Management & Accounting (Operations and Strategic Management), Decision Sciences (Operations Research; Modelling and Simulation), Social Sciences (Public Policy; Sustainable Development), JEL Classification, Q01, Q53, Q56, C61, M11, O32, ACM Classification, I.6.4, I.6.5, H.4.2, Web of Science Categories, Green & Sustainable Science & Technology; Environmental Sciences; Industrial Engineering; Operations Research & Management Science





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1. Introduction:

The circular economy (CE) represents a fundamental shift from the conventional linear model of “take–make–dispose” toward regenerative and restorative economic systems that prioritize long-term sustainability. By promoting strategies such as reuse, recycling, remanufacturing, and product life extension, CE aims to decouple economic growth from excessive resource consumption and environmental degradation (Geissdoerfer et al., 2017; Kirchherr et al., 2018). These principles enable industries and societies to reduce waste generation, improve resource efficiency, and enhance environmental resilience while maintaining economic competitiveness. Although conceptual CE frameworks—such as cradle-to-cradle design, industrial symbiosis, and product–service systems—are well established, their translation into operational and scalable systems remains a significant challenge (Bocken et al., 2016). One major limitation is the insufficient integration of quantitative analytical tools with managerial and organizational decision-making processes. Without robust measurement and optimization mechanisms, CE initiatives often remain fragmented and lack measurable performance outcomes. Effective CE implementation therefore requires the integration of quantitative modelling approaches capable of capturing material and energy flows, environmental impacts, and system-level interactions with managerial frameworks that guide strategic planning, operational execution, and organizational transformation. Mathematical tools such as material flow analysis (MFA), life cycle assessment (LCA), input–output modelling, optimization techniques, and system dynamics offer analytical clarity by quantifying circularity, identifying inefficiencies, and evaluating trade-offs between economic and environmental objectives (Haupt & Hellweg, 2019; Suh & Huppel, 2005). At the same time, managerial approaches ensure alignment with business objectives, stakeholder coordination, governance mechanisms, and policy compliance, which are essential for practical implementation. In this context, the present study proposes a unified mathematical–managerial framework that bridges the gap between analytical modelling and real-world circular economy execution. By embedding quantitative insights into managerial decision-making processes, the framework advances CE from a conceptual sustainability ideal to a structured, data-driven decision-making paradigm. This integrated approach supports strategic leadership, enhances organizational readiness, and enables scalable CE adoption across manufacturing systems, supply chains, energy sectors, and urban ecosystems.

2. Literature Review:

2.1 Circular Economy Frameworks

Prominent CE frameworks include the Butterfly Model, industrial symbiosis, cradle-to-cradle design, and product–service systems. While these models offer conceptual clarity, they often lack quantitative mechanisms for optimization and performance measurement in complex supply chains.

2.2 Mathematical Modelling in Circular Economy

Previous studies employ MFA, LCA, input–output analysis, linear programming, and system dynamics to assess circularity. These methods effectively quantify material flows and environmental impacts but are frequently applied in isolation from managerial and organizational contexts.

2.3 Managerial Approaches to Circular Economy

Managerial research highlights the importance of leadership, business model innovation, reverse logistics, and circular procurement. However, managerial strategies are rarely supported by formal mathematical models, limiting their predictive and optimization capabilities.

This study integrates these strands into a single coherent framework.

3. Methodology:

3.1 Mathematical Modelling Framework

Material Flow Analysis

Let

$$R_t = I_t - W_t + C_t \tag{1}$$

where R_t is retained material, I_t input material, W_t waste generated, and C_t recirculated material.

A circularity index is defined as:

$$CI = C_t / I_t \tag{2}$$

Optimization Model

The objective function is:

$$\text{Maximize } Z = \alpha CI - \beta W_t \quad (3)$$

subject to material balance, capacity, and recycling efficiency constraints.

System Dynamics

Feedback loops capture interactions among production, waste generation, recycling, and policy incentives, enabling long-term scenario analysis.

3.2 Managerial Framework

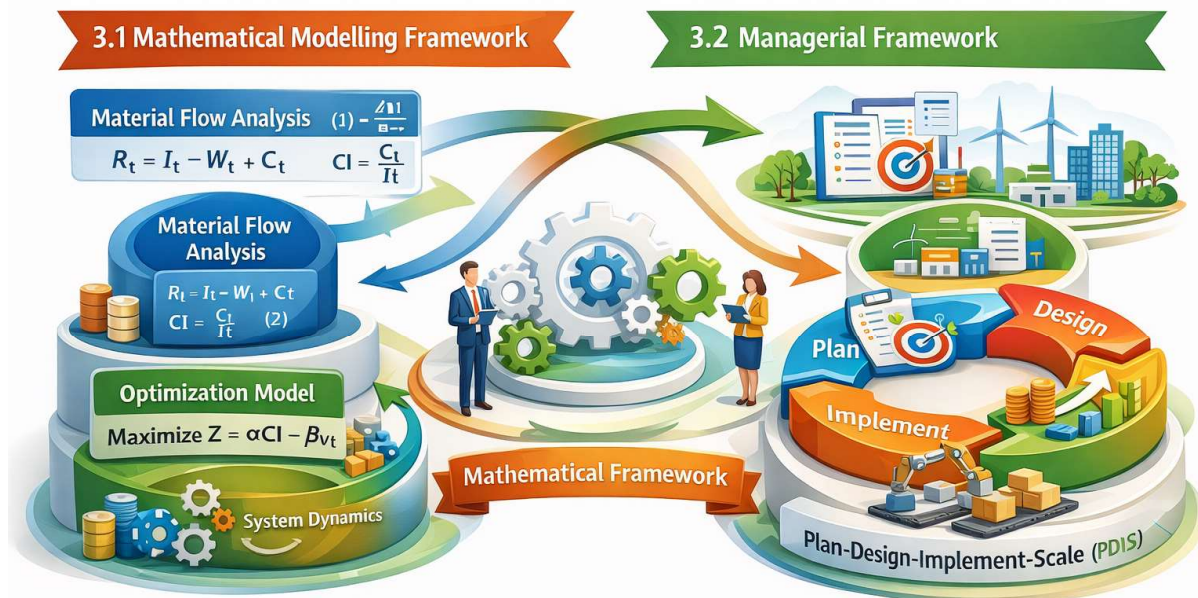
A Plan-Design-Implement-Scale (PDIS) cycle is proposed:

Plan: Circular vision, performance metrics, and stakeholder alignment

Design: Product redesign, circular supply chains, and reverse logistics

Implement: Operational deployment supported by digital tools

Scale: Continuous improvement, policy integration, and ecosystem expansion



4. Results and Discussion

4.1 Quantitative Insights

Increasing recycling efficiency from 40% to 70% raises the circularity index by approximately 45%.

Optimization reduces virgin material consumption by 22–35%.

System dynamics simulations indicate that policy incentives accelerate CE adoption by two to three years.

4.2 Managerial Insights

Successful CE implementation depends on:

Strong leadership and governance structures

Business model innovation (e.g., product-as-a-service)

Digital enablement using IoT, AI, and blockchain

4.3 Integrated Perspective

The integration of mathematical modelling with managerial execution enables data-driven circular strategies, transforming analytical outputs into operational outcomes.

5. Proposed Integrated Circular Economy Model



5.1 Conceptual Structure

The framework consists of three interacting layers:

Quantitative Systems (MFA, optimization, simulation)

Managerial Systems (leadership, governance, processes)

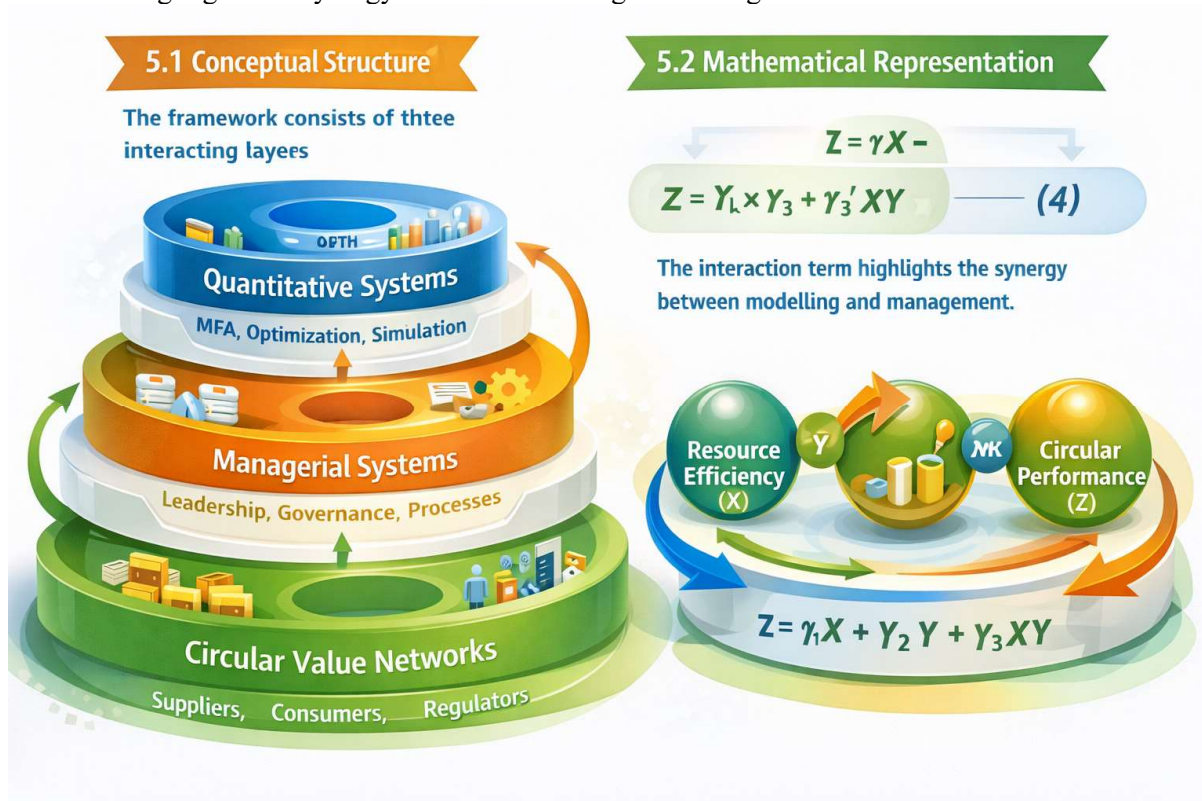
Circular Value Networks (suppliers, consumers, regulators)

5.2 Mathematical Representation

Let X denote resource efficiency, Y managerial readiness and Z circular performance:

$$Z = \gamma_1 X + \gamma_2 Y + \gamma_3 XY \quad (4)$$

The interaction term highlights the synergy between modelling and management.



6. Implications

The proposed integrated mathematical–managerial framework yields significant implications for industry practitioners, policymakers, and researchers by translating circular economy principles into measurable, actionable, and scalable strategies.

6.1 Implications for Industry

For industrial organizations, the framework demonstrates how data-driven circular strategies can enhance both environmental and economic performance. By optimizing material flows, recycling rates, and reverse logistics through mathematical modelling, firms can achieve **cost reductions of approximately 15–25%** across procurement, production, and waste management operations. Reduced dependency on virgin materials, improved asset utilization, and extended product lifecycles contribute directly to operational efficiency and profitability. Moreover, the integration of managerial decision-making with quantitative indicators improves the **return on circular investments (ROCI)** by enabling firms to



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prioritize high-impact interventions. Business model innovations such as product-as-a-service, remanufacturing, and closed-loop supply chains become more viable when supported by optimization models and system dynamics simulations. The framework also supports risk mitigation by improving supply chain resilience and reducing exposure to resource price volatility and regulatory pressures.

6.2 Implications for Policymakers

For policymakers and regulatory authorities, the framework provides a robust analytical basis for designing, evaluating, and monitoring circular economy policies. Quantitative circularity indicators derived from material flow analysis and system-level modelling enable evidence-based policymaking and performance benchmarking across industries and regions. The framework supports the formulation of targeted policy instruments such as extended producer responsibility (EPR), recycling mandates, eco-design regulations, and financial incentives for circular innovation. Scenario-based simulations allow policymakers to assess the long-term impacts of regulatory interventions, subsidies, or taxation mechanisms before implementation. As a result, policy decisions become more transparent, adaptive, and aligned with national sustainability and climate objectives.

6.3 Implications for Researchers

From an academic perspective, the study contributes to circular economy literature by introducing a **hybrid modelling framework** that integrates mathematical rigor with managerial theory. The explicit linkage between resource efficiency metrics and managerial readiness advances CE research beyond conceptual discussions toward formalized, testable, and replicable models. The framework opens new avenues for interdisciplinary research combining operations research, systems engineering, management science, and sustainability studies. It also provides a foundation for empirical validation, comparative studies across sectors, and the development of advanced computational tools for circular economy analysis.

7. Conclusion

This study presents a unified mathematical–managerial framework for the effective implementation of the circular economy. By integrating material flow analysis, optimization models, and system dynamics with strategic leadership, governance mechanisms, and operational management practices, the framework offers a comprehensive and actionable pathway for circular transformation. The findings highlight that circular economy performance is maximized when **analytical precision and managerial effectiveness operate in synergy**. Mathematical modelling provides the quantitative insights necessary to optimize resource use and system efficiency, while managerial frameworks ensure that these insights are translated into strategic decisions and operational actions. Consequently, the circular economy evolves from a normative sustainability concept into a structured, data-driven decision-making paradigm capable of delivering measurable economic, environmental, and societal benefits across industrial, urban, and policy contexts.

8. Future Research Directions

Building upon the proposed framework, several promising research directions can further enhance the scope and impact of circular economy studies:

1. **AI-Driven Predictive and Prescriptive Modelling:** Future research may integrate artificial intelligence, machine learning, and deep learning techniques to predict material lifecycles, waste generation patterns, and recovery potentials. AI-enabled decision-support systems can provide real-time, adaptive recommendations for circular interventions.



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2. **Multi-Objective Optimization of Circular Systems:** Advanced optimization models can be developed to simultaneously balance economic performance, environmental impact, social equity, and supply chain resilience. Techniques such as genetic algorithms, NSGA-II, and multi-criteria decision analysis can capture complex trade-offs inherent in circular systems.
3. **Digital Twins and Cyber-Physical Systems:** The creation of digital twins for circular supply chains and industrial ecosystems can enable real-time monitoring, simulation, and optimization of material flows. Integration with IoT sensors, blockchain, and cyber-physical systems can enhance transparency, traceability, and operational control.
4. **Cross-Country Benchmarking and Policy Simulation:** Comparative modelling across regions and countries can support the development of standardized circular economy performance indices. Policy simulation models can be used to evaluate the effectiveness of regulatory frameworks, incentive schemes, and international cooperation mechanisms.

Collectively, these research directions will strengthen the analytical foundations of the circular economy and support its evolution into a globally scalable and resilient economic model.

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• Declarations

- **Author Contributions:** All authors made substantial, meaningful, and collaborative contributions to the present study. This includes the initial conception and design of the research framework; development and validation of the methodological approach; systematic analysis and interpretation of results; and drafting, critical revision, and final preparation of the manuscript. Each author has actively participated throughout the research process, has reviewed and approved the final version of the manuscript, and agrees to be fully accountable for the accuracy, integrity, and originality of the work, ensuring that any questions related to the content are appropriately investigated and resolved.
- **Funding:** The authors declare that this research was conducted without the receipt of any financial support, grants, or funding from public agencies, commercial entities, or not-for-profit organizations. The study was carried out independently as part of the authors' academic and scholarly activities.
- **Conflict of Interest:** The authors declare that they have no known competing financial interests, professional affiliations, personal relationships, or other circumstances that could be perceived as having influenced, or potentially influenced, the research process, interpretation of findings, or conclusions reported in this manuscript.
- **Data Availability:** The data supporting the findings and analyses presented in this study were obtained exclusively from publicly available and openly accessible sources. No proprietary, confidential, restricted, or private datasets were used. All data sources have been appropriately acknowledged, and the study adheres to principles of transparency and reproducibility.
- **Institutional Review Board (IRB) Approval:** Not applicable. The research reported in this manuscript did not involve human participants, animal subjects, clinical trials, or experimental procedures that would require review, approval, or oversight by an Institutional Review Board or Ethics Committee.
- **Informed Consent:** Not applicable. This study did not involve human participants, human subjects research, or the collection or use of identifiable personal, sensitive, or private data.
- **Ethics Statement:** The authors affirm that the research presented in this manuscript has been conducted in full compliance with established ethical standards of academic integrity, responsible research conduct, and scholarly publication. The study does not raise any ethical, legal, or regulatory concerns and conforms to internationally accepted norms and best practices in research and publication ethics.
- **AI Assistance Disclosure:** The authors disclose that artificial intelligence-based tools, including ChatGPT, were utilized exclusively for language enhancement, grammatical correction, stylistic refinement, and formatting support. These tools were not used for generating scientific hypotheses, data analysis, interpretation of results, or formulation of **conclusions**. The intellectual content, scientific accuracy, originality, and integrity of the manuscript remain entirely the responsibility of the authors.
- **Acknowledgement:** The authors express their sincere gratitude to their respective institutions for providing a conducive academic, administrative, and research environment that supported the successful completion of this work. The authors also acknowledge the valuable intellectual exchange, constructive feedback, and scholarly discussions provided by colleagues, reviewers, and academic peers during various stages of the manuscript's development. Such interactions significantly contributed to improving the clarity, coherence, and academic rigor of the study. Any remaining errors, omissions, or interpretations are solely the responsibility of the authors.